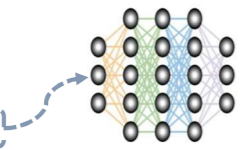
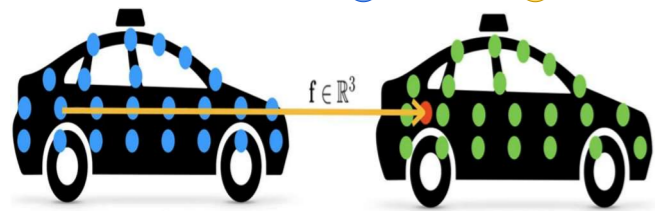


## Background: Neural Scene Flow Prior

"Spatially smooth" scene flow via the smoothness bias of the coordinate MLP



$$\theta^* = \operatorname{argmin}_{\theta} \mathcal{L}_{CD}(\mathbf{P}_1 + \Phi(\mathbf{P}_1; \theta), \mathbf{P}_2)$$

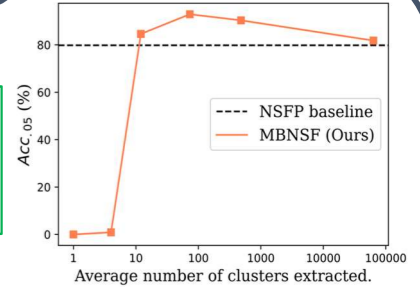


## Can we enforce multi-body rigidity in neural scene flow without:

- Sacrificing the continuous flow field?
- Constraining the  $SE(3)$  parameters of each rigid body?
- Accurately estimating the rigid bodies?

## Results Quantitative

Robust to over-clustering  $\Rightarrow$  Accurate rigid body estimation is not needed



Performance improvement on any dataset, on any number of points

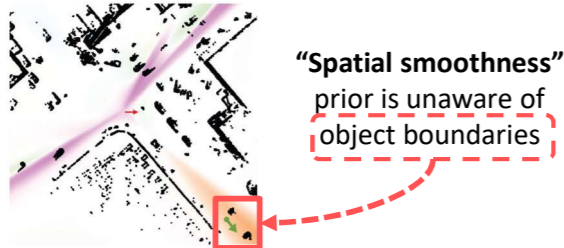
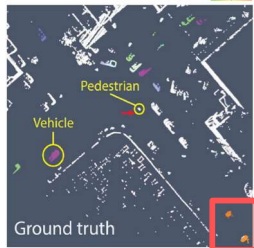
Dataset	Method	Supervision	Num. Points	EPE [m] ↓	Acc <sub>0.5</sub> [%] ↑	Acc <sub>1.0</sub> [%] ↑	θ <sub>1</sub> [°] ↓
Waymo	FLOT [37]	Full	8192	0.702	2.46	11.30	0.808
	PointPWC-Net [54]	Self	8192	4.109	0.05	0.36	1.742
	WsRSF [16]	Weak	8192	0.414	35.47	44.96	0.527
	NSFP [26]	None	8192	0.098	69.34	85.95	0.302
	MBNSF (Ours)	None	8192	<b>0.097</b>	<b>74.15</b>	<b>89.24</b>	<b>0.295</b>
	NSFP [26]	None	All	0.091	76.61	89.00	0.282
Argoverse	FLOT [37]	Full	8192	0.796	2.30	9.87	0.929
	PointPWC-Net [54]	Self	8192	5.724	0.02	0.15	1.147
	WsRSF [16]	Weak	8192	0.416	34.52	43.10	0.558
	NSFP [26]	None	8192	0.056	70.30	89.57	0.265
	MBNSF (Ours)	None	8192	<b>0.051</b>	<b>79.36</b>	<b>92.37</b>	<b>0.264</b>
	NSFP [26]	None	All	0.090	64.97	83.09	0.230
MBNSF (Ours)	None	All	<b>0.033</b>	<b>89.34</b>	<b>95.91</b>	<b>0.168</b>	

Supports both pairwise scene flow and direct 4D trajectory estimation

Approach	Method	Acc <sub>0.5</sub> [%] ↑	Acc <sub>1.0</sub> [%] ↑
Scene flow integration (forward-Euler)	NSFP [47]*	45.28	59.52
	NSFP†	38.09	54.20
	<b>MBNSF (Ours)</b>	<b>61.11</b>	<b>74.34</b>
Direct 4D trajectory prediction	NTP [47]*	52.28	69.88
	NTP†	48.06	62.45
	<b>MBNT (Ours)</b>	<b>59.82</b>	<b>73.57</b>

## Motivation: Rigidity in Neural Scene Flow

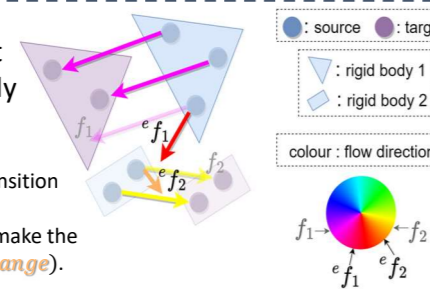
Ground-truth Neural flow field



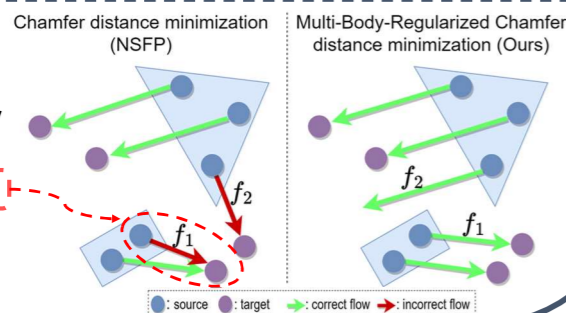
"Spatial smoothness" prior is unaware of object boundaries

Enforcing smoothness at object boundaries may lead to physically implausible flow predictions

- Ground-truth flow contains a sharp transition from  $f_1$  (purple) to  $f_2$  (yellow).
- The neural prior tends to (incorrectly) make the transition smooth -  $e_{f_1}$  (red) to  $e_{f_2}$  (orange).



Chamfer distance optimization may violate multi-body rigidity due to nearest neighbor correspondence assignment

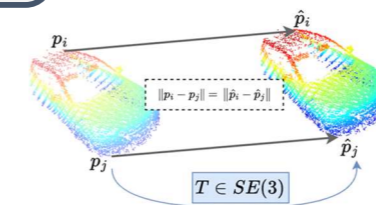


## Approach: Rigid flow via isometry

### Key insight:

The flow of rigid bodies should maintain an isometry

$$\|p_i - p_j\| = \|\hat{p}_i - \hat{p}_j\| \quad \forall i, j \implies \hat{p}_i = \mathbf{T} \circ p_i \quad \forall i.$$



Encouraging isometry in the flow predictions for rigid bodies will ensure  $SE(3)$  rigidity without having to estimate/constrain the  $SE(3)$  parameters

### Formulation:

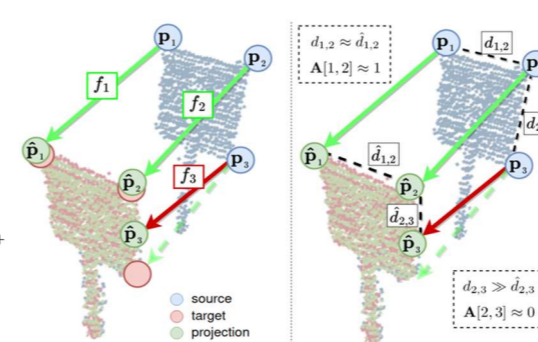
For each rigid body, score  $s(\mathbf{C}, \mathbf{F})$  represents the degree of preservation of isometry for its point cluster  $\mathbf{C}$  and its associated flow prediction  $\mathbf{F}$ .

$$s(\mathbf{C}, \mathbf{F}) = \frac{1}{n} \mathbf{v}^* \mathbf{T} \mathbf{A} \mathbf{v}^*$$

$$A[i, j] = \left[ 1 - \frac{(d_{i,j} - \hat{d}_{i,j})^2}{d_{thr}^2} \right]_+$$

$$s(\mathbf{C}, \mathbf{F}) = 1 \implies \text{exact isometry}$$

$$0 < s(\mathbf{C}, \mathbf{F}) < 1 \implies \text{approximate isometry}$$



### Final objective:

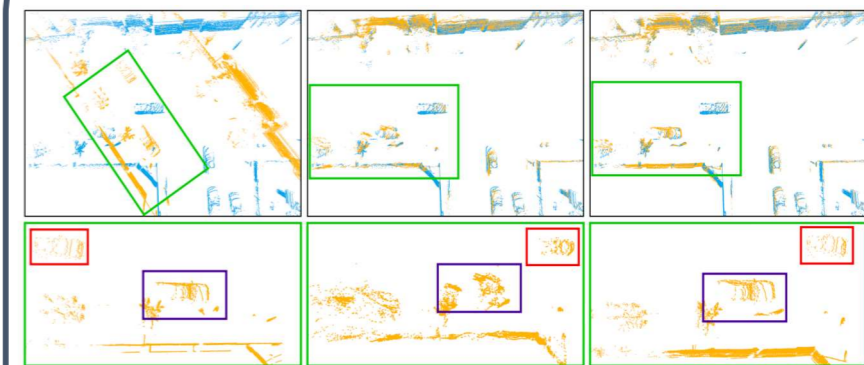
Maximize the score  $s(\mathbf{C}, \mathbf{F})$  for all clusters in the scene while reducing Chamfer distance.

$$\theta^* = \operatorname{argmin}_{\theta} \mathcal{L}_{CD}(\mathbf{P}_1 + \Phi(\mathbf{P}_1; \theta), \mathbf{P}_2) + \omega \cdot \mathcal{L}_{MB}(\mathbf{P}_1; \theta)$$

$$\text{where } \mathcal{L}_{MB}(\mathbf{P}_1; \theta) = -\log(s_{avg}(\mathbf{P}_1; \theta))$$

$$s_{avg}(\mathbf{P}_1; \theta) = \frac{1}{m} \sum_{i=1}^m s(\mathbf{C}_i, \mathbf{F}_i)$$

## Results Qualitative



Preserves multi-body rigidity, even across long sequences.

## Implementation

Our code is publicly available:

